## The $M_3$ versus $M_1$ Problem

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In this talk we state and discuss a very old problem, commonly known as the  $M_3$  versus  $M_1$  problem. Some related thoughts in the setting of ordered topological spaces will be presented. We show that if  $(X, \mathcal{T}, \leq)$  is an ordered metrizable topological C-and I-space then the bitopological space  $(X, \mathcal{T}^{\natural}, \mathcal{T}^{\flat})$  is pairwise  $M_3$ . [Here,  $\mathcal{T}^{\natural} := \{U \in \mathcal{T} \mid U \text{ is an upper set}\}$  and  $\mathcal{T}^{\flat} := \{L \in \mathcal{T} \mid L \text{ is a lower set}\}$ .]