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The semicontinuous quasi-uniformity of a frame, revisited. (English summary)

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The semicontinuous quasi-uniformity of a frame generalizes the semicontinuous quasi-uniformity of a topological space (known to be one of the most important examples of transitive compatible quasi-uniformities).

The aim of this paper is to provide a new treatment of the results obtained by the authors in a previous paper [Kyungpook Math. J. **46** (2006), no. 2, 189–200; MR2235558 (2006m:54050)].

The authors show how the ring of arbitrary (not necessarily continuous) real-valued functions on a frame introduced in [J. Gutiérrez García, T. Kubiak and J. Picado, J. Pure Appl. Algebra **213** (2009), no. 6, 1064–1074; MR2498797 (2010a:06020)] can be used to present these results in a nice way.

Reviewed by *Javier Gutiérrez García*

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Note: This list reflects references listed in the original paper as accurately as possible with no attempt to correct errors.