

```
In[1]:= Clear["Global`*"];
LFT3[z_, z1_, z2_, z3_] := (z - z1) * (z2 - z3) / ((z - z3) * (z2 - z1));
```

```
In[3]:= Simplify[Solve[LFT3[w, -1, -I, 1] == LFT3[z, 0, 1, 2], w]]
```

$$\text{Out}[3]= \left\{ \left\{ w \rightarrow \frac{\frac{i}{2} (-1 - i) + z}{(-1 + i) + z} \right\} \right\}$$

```
In[4]:= wa = Simplify[Solve[LFT3[w, -1, -I, a] == LFT3[z, 0, 1, 2], w]]
```

$$\text{Out}[4]= \left\{ \left\{ w \rightarrow \frac{a (2 - (2 - i) z) - i (-2 + z)}{-2 i + a (-2 + z) - (1 - 2 i) z} \right\} \right\}$$

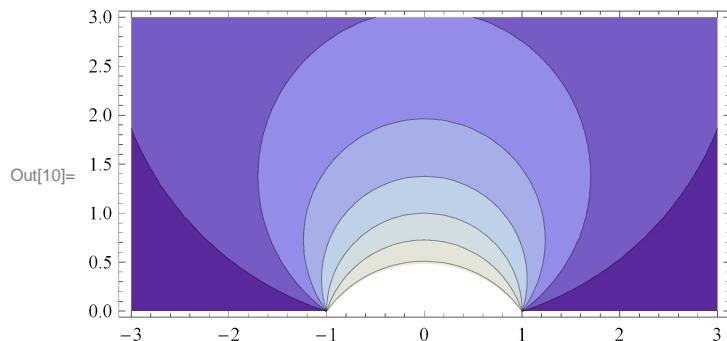
```
In[5]:= w = w /. wa[[1]]
```

$$\text{Out}[5]= \frac{a (2 - (2 - i) z) - i (-2 + z)}{-2 i + a (-2 + z) - (1 - 2 i) z}$$

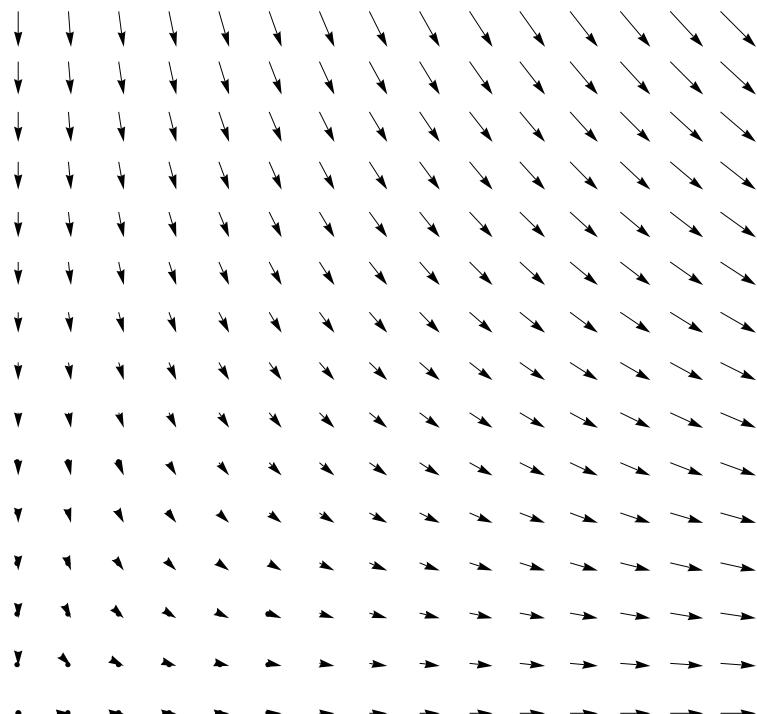
```
In[6]:= Limit[w, a → ComplexInfinity]
```

$$\text{Out}[6]= \frac{2 - (2 - i) z}{-2 + z}$$

```
In[7]:= x /: Im[x] = 0; y /: Im[y] = 0;
v = Im[Log[(z - 1)/(z + 1) /. z → x + I*y]];
u = Re[Log[(z - 1)/(z + 1) /. z → x + I*y]];
T = v/Pi; ContourPlot[T, {x, -3, 3}, {y, 0.001, 3},
AspectRatio → Automatic]
```



```
In[11]:= Needs["VectorFieldPlots`"];
Needs["VectorFieldPlots`"];
HamiltonianFieldPlot[2 x y, {x, 0, 2}, {y, 0, 2}]
```



```
Out[13]=
```

```
In[14]:= Off[General::obspkg]; Off[General::newpkg]; Needs["Graphics`ImplicitPlot`"];  
AA = ImplicitPlot[  
  {y (1 - 1 / (x^2 + y^2)) == .0,  
   y (1 - 1 / (x^2 + y^2)) == .2,  
   y (1 - 1 / (x^2 + y^2)) == .4,  
   y (1 - 1 / (x^2 + y^2)) == .6,  
   y (1 - 1 / (x^2 + y^2)) == .8,  
   y (1 - 1 / (x^2 + y^2)) == 1.0,  
   y (1 - 1 / (x^2 + y^2)) == 1.2,  
   y (1 - 1 / (x^2 + y^2)) == -.2,  
   y (1 - 1 / (x^2 + y^2)) == -.4, y (1 - 1 / (x^2 + y^2)) == -.6,  
   y (1 - 1 / (x^2 + y^2)) == -.8,  
   y (1 - 1 / (x^2 + y^2)) == -1.0,  
   y (1 - 1 / (x^2 + y^2)) == -1.2}, {x, -2, 2},  
  Axes -> False, DisplayFunction -> Identity];  
fluid = Show[AA, DisplayFunction -> $DisplayFunction]
```

