Categorical aspects of K-theory for operator algebras

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We present some categorical aspects of K-theories for operator algebras (K, KK and E) that have played a crucial role in the development of the field.

A compelling example is the way the question if Kasparov's bivariant K-theory is exact or not, was tackled. The negative answer was provided by Skandalis by means of an example, but meanwhile Higson had shown that such a theory exists. A concrete description have been found by Connes and Higson using asymptotic morphisms, which later have been used as the main ingredient in the proof of the Baum-Connes conjecture for amenable groups.

We present some results in the equivariant setting, and some related questions which have appeared lately.

References

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