On Morita Equivalence of Categories

Bertalan Pécsi

We introduce the notion of *bridge* between categories, and show how *profunctors* and, in particular, *adjoint* pairs of functors can be interpreted as special bridges. Using this technique of profunctors and bridges we prove that two categories are *equivalent* [resp. *Morita equivalent*] if and only if there exist a certain kind of bridge between them.

The case of Morita equivalence also gives an elegant proof of the classical result:

Let \mathcal{A} and \mathcal{B} be categories. We show that statements a) and c) below are both equivalent to b).

- a) There is an invertible profunctor between \mathcal{A} and \mathcal{B} .
- b) There is a so called Morita-bridge between \mathcal{A} and \mathcal{B} .
- c) The idempotent (or Cauchy) completions of \mathcal{A} and \mathcal{B} are equivalent.

References

 Bertalan Pécsi, On Morita Equivalence of Rings and Categories, preprint www.renyi.hu/~aladar (2007) 1-8.