Plane trees and higher categories

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This is joint work with Michael Batanin on consequences of his construction, in terms of plane trees, of the free strict omega-category on a globular set. The generated monad M on globular sets shares many of the properties of the word monad on sets. Benabou's construction [Lecture Notes in Math. 1488 (Springer, 1991) pages 28-29] of the algebraic simplicial category (finite ordinals) from the word monad can be copied for M to yield a globular category which is our main object of study. There is a universal property corresponding to Lawvere's universal property of finite ordinals and there is an alternative description related to Joyal's approach to weak omegacategories.