

# On some mysterious Mal'tsev conditions and the associated imaginary co-operations

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We prove that varietal techniques based on the existence of operations of a certain arity can be extended to  $n$ -permutable categories with finite coproducts using a method developed by D. Bourn and Z. Janelidze [1]. In particular, we give a categorical version of the characterisation theorems for  $n$ -permutable varieties due to J. Hagemann and A. Mitschke [3].

## References

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