

Strict monadic topology: first separation axioms and reflections

Given a monad T on the category of sets, we consider reflections of $\text{Alg}(T)$ into the full subcategories formed by algebras satisfying natural counterparts of topological separation axioms T_0, T_1, T_2 and T_{ts} (where “ts” stands for “totally separated”). We ask whether these reflections satisfy simple conditions useful in categorical Galois theory, and we give some partial answers in easy cases; for that, we use Birkhoff’s well-known characterization of distributive lattices [1], and some results of [2]-[5].

References

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