# Spaces with an $M$-diagonal

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In this talk we will prove that if $X$ is a Tychonoff space and $X^2 \setminus \Delta$ is dominated by a second countable space then $X$ is cosmic. This solves an open problem of Cascales, Orihuela and Tkachuk (see[COT]). We also consider the case when $X$ is compact and $X^2 \setminus \Delta$ is dominated by a metric space $M$; in this situation we show that if such domination is strong, then the tightness of $X$ is bounded by the weight of $M$

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